

Isochrons

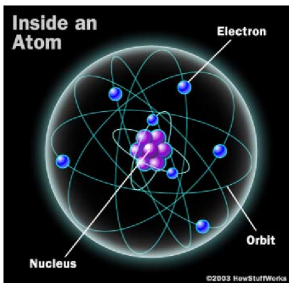
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September 12, 2013

Outline

- ▶ What is radioactive decay?
- ▶ Why it measures time.
- ▶ Objections
 - ▶ Don't we have to know the rock's initial composition?
- ▶ Isochrons

Atom

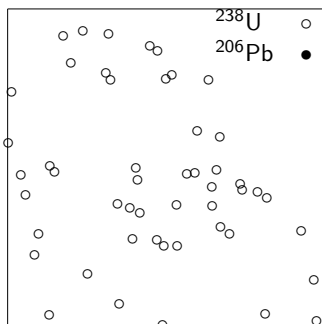


- ▶ electron shell
- ▶ nucleus
 - ▶ protons (determine which element)
 - ▶ neutrons
 - ▶ protons + neutrons = mass

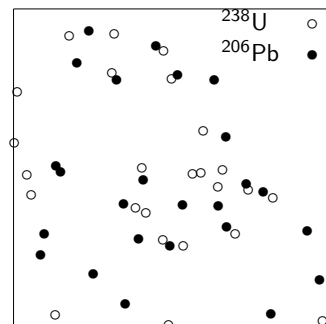
Isotopes

- ▶ Some atoms of oxygen (or any other element) weigh more than others.
- ▶ These variants are *isotopes*.
- ▶ Some isotopes are stable.
- ▶ Others are unstable, or radioactive.
- ▶ Atoms of a radioactive isotope tend to decay into something else.

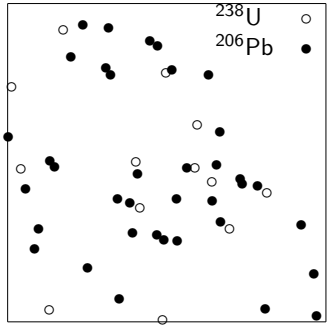
An initial collection of atoms



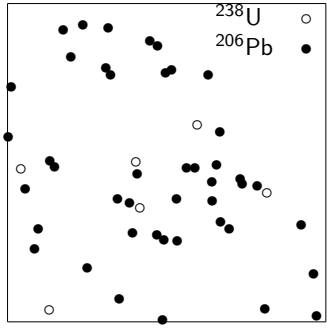
After 1 half-life



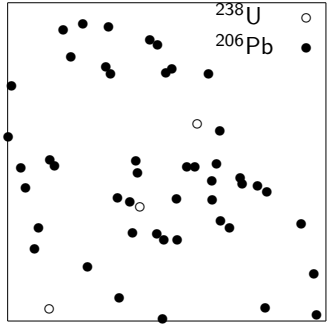
After 2 half-lives



After 3 half-lives



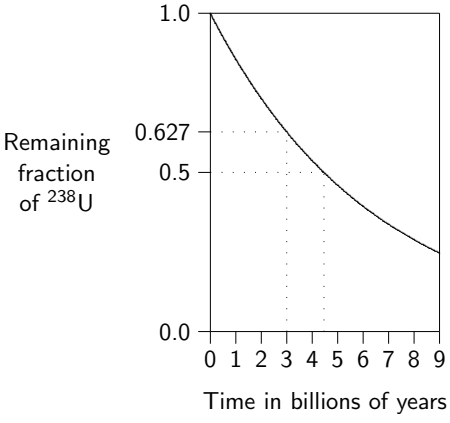
After 4 half-lives



Some radioactive isotopes used in dating

Element	Isotope	half-life
Carbon	^{14}C	$5.730 \times 10^3 \text{ y}$
Potassium	^{40}K	$1.248 \times 10^9 \text{ y}$
Uranium	^{238}U	$4.468 \times 10^9 \text{ y}$
Rubidium	^{87}Rb	$4.92 \times 10^{10} \text{ y}$

Radiometric clock, using ^{238}U



The fraction of ^{238}U remaining tells us how much time has elapsed.

$0.627 \implies 3 \text{ byr}$

$0.5 \implies 4.468 \text{ byr}$

Objection

How can we tell what fraction remains unless we know how much was originally there?

Outline

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- ▶ Why it measures time.
- ▶ Objections
 - ▶ Don't we have to know the rock's initial composition?
- ▶ Isochrons

Hypothetical example

- ▶ Begins with three samples from a rock that formed 4.46 billion years ago—the half-life of ^{238}U .
- ▶ We will see original isotope ratios, and also those in modern rock.
- ▶ We will estimate age from modern ratios.

When rock was formed

Columns B–C show the number of atoms of each isotope.

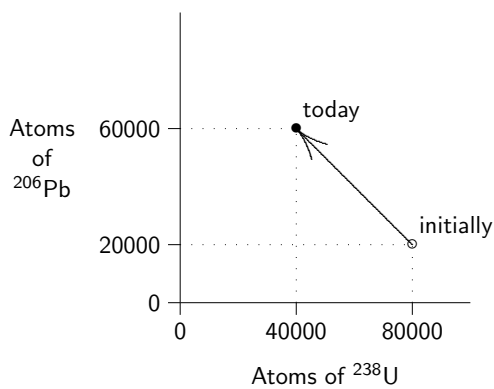
A	B	C
Samp.	^{238}U	^{206}Pb
1	80000	20000
2	30000	10000
3	90000	50000

Today

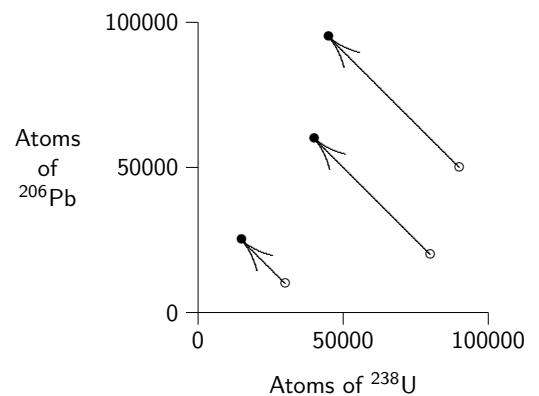
Columns B–C show the number of atoms of each isotope.

A	B	C
Samp.	^{238}U	^{206}Pb
1	40000	60000
2	15000	25000
3	45000	95000

Change in sample 1



All three samples



Adding an inert isotope

- ▶ ^{204}Pb does not decay.
- ▶ Nothing decays into ^{204}Pb .
- ▶ The number of ^{204}Pb atoms is unchanging.
- ▶ Let us add ^{204}Pb to the data table.

When rock was formed

1 atom of ^{204}Pb for every 15 of ^{206}Pb .

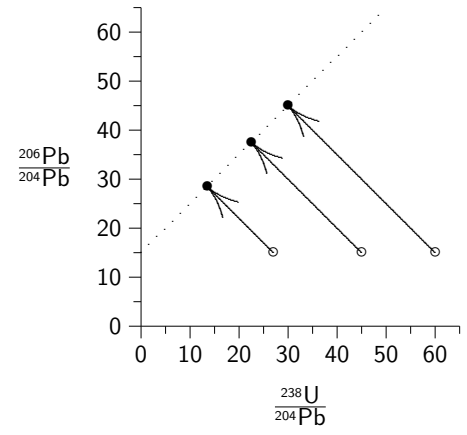
A	B	C	D	E	F
Samp.	^{238}U	^{206}Pb	^{204}Pb	$\frac{^{238}\text{U}}{^{204}\text{Pb}}$	$\frac{^{206}\text{Pb}}{^{204}\text{Pb}}$
1	80000	20000	1333	60	15
2	30000	10000	667	45	15
3	90000	50000	3333	27	15

Today

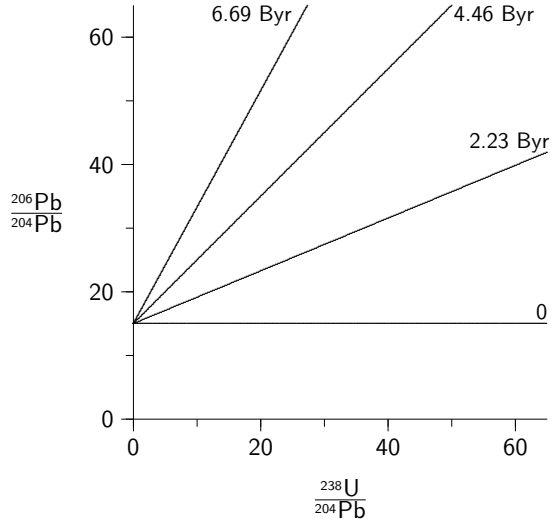
Number of atoms of ^{204}Pb doesn't change.

A	B	C	D	E	F
Samp.	^{238}U	^{206}Pb	^{204}Pb	$\frac{^{238}\text{U}}{^{204}\text{Pb}}$	$\frac{^{206}\text{Pb}}{^{204}\text{Pb}}$
1	40000	60000	1333	30.0	45.0
2	15000	25000	667	22.5	37.5
3	45000	95000	3333	13.5	28.5

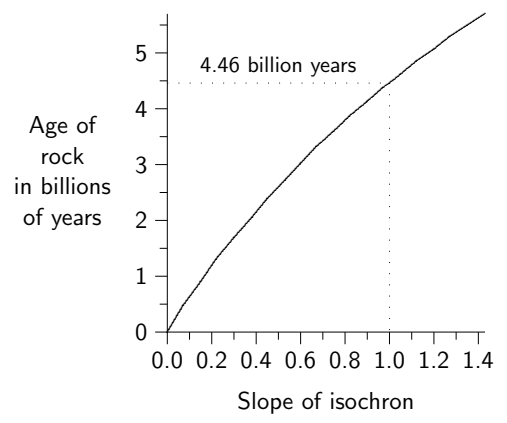
Isochron



Slope of isochron shows age of rock



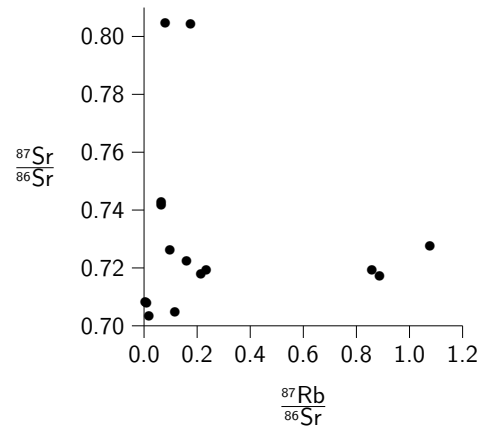
Slope of isochron shows age of rock



Objection

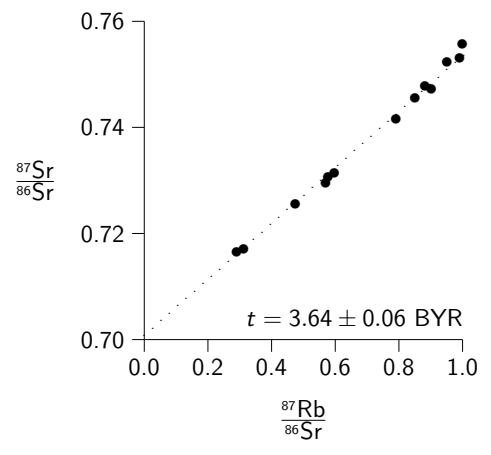
What if you lose or gain something?

When the assumptions fail

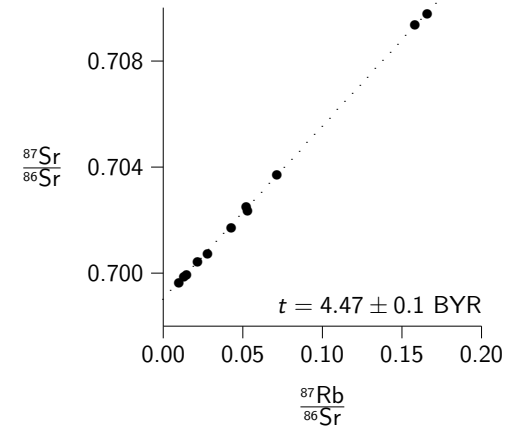


When the assumptions hold

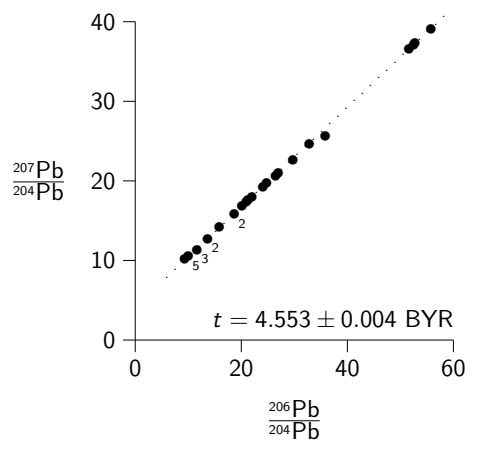
Greenland gneiss



Moon rock



Allende meteorite



Summary

- ▶ Radioactive decay is clock-like
- ▶ Isochrons avoid the problem of the rock's unknown initial condition.
- ▶ When the isochron's assumptions fail, you can tell.
- ▶ The oldest known rocks are:

Age (Byr)	
4.4	Australia
4.47	Moon
4.55	Meteorites